



Optimal control of Polar Active Fluid

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Model

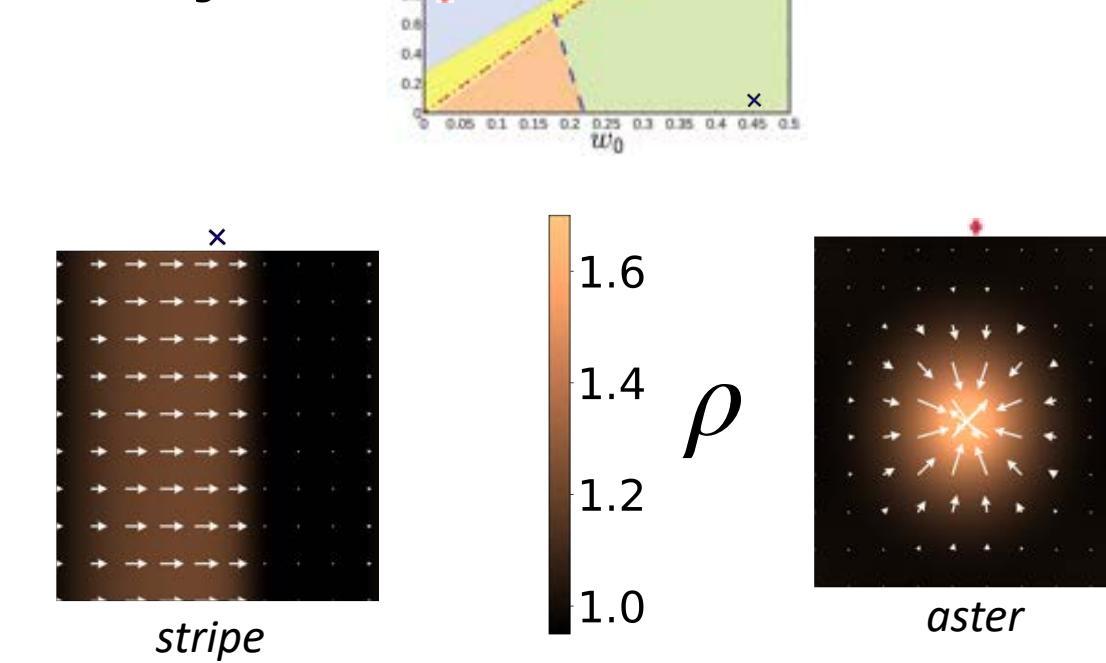
$\rho(\mathbf{r})$ – Density
 $\vec{P}(\mathbf{r})$ – Polarization
 $\vec{\tau} = \rho \vec{P}$

Polar aligning interaction

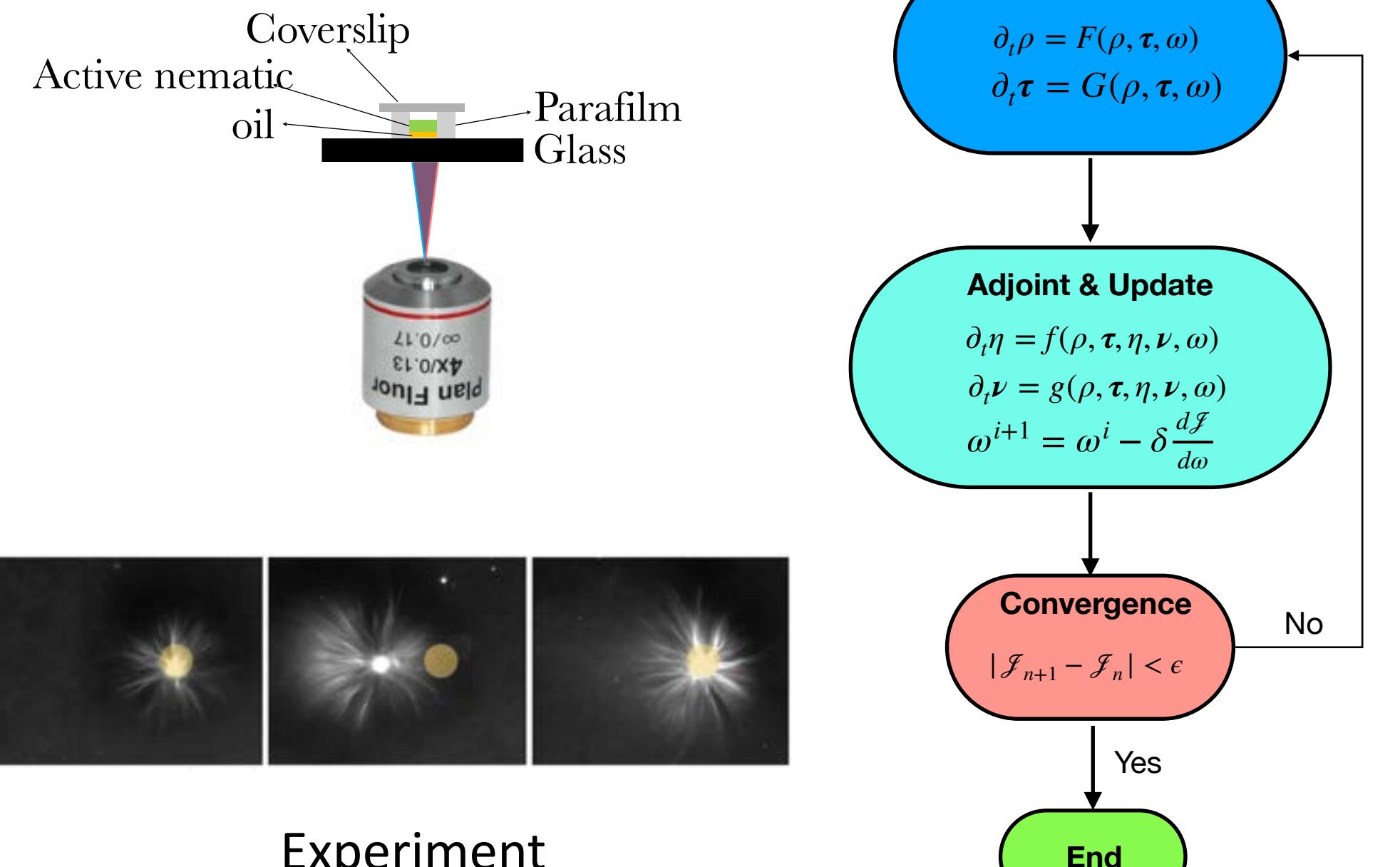
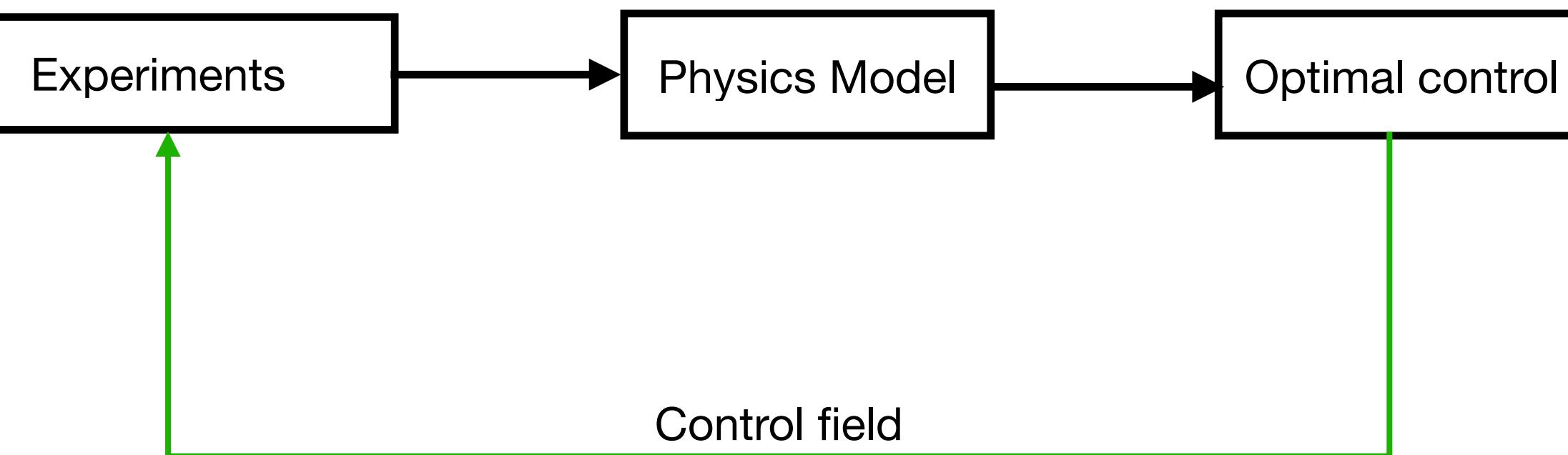
$$\partial_t \rho = -\nabla \cdot (\omega \vec{\tau} - \nabla \rho).$$

$$\partial_t \vec{\tau} = -(a_2(\rho) + a_4(\rho) |\vec{\tau}|^2) \vec{\tau} - \nabla(\omega \rho) + \nabla^2 \vec{\tau} + \lambda (\tau_\alpha \nabla \tau_\alpha + \vec{\tau} \nabla \cdot \vec{\tau} - \vec{\tau} \cdot \nabla \vec{\tau}).$$

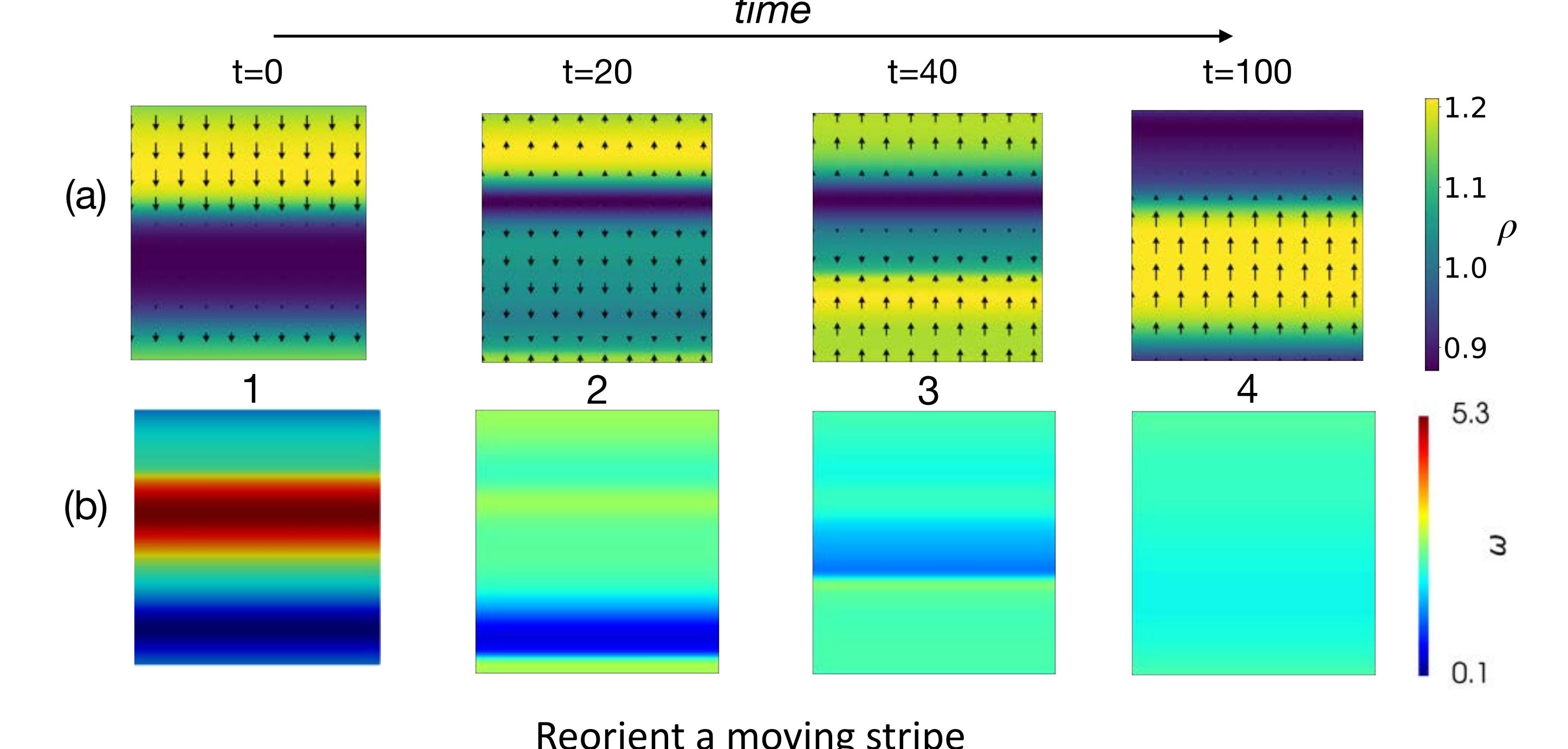
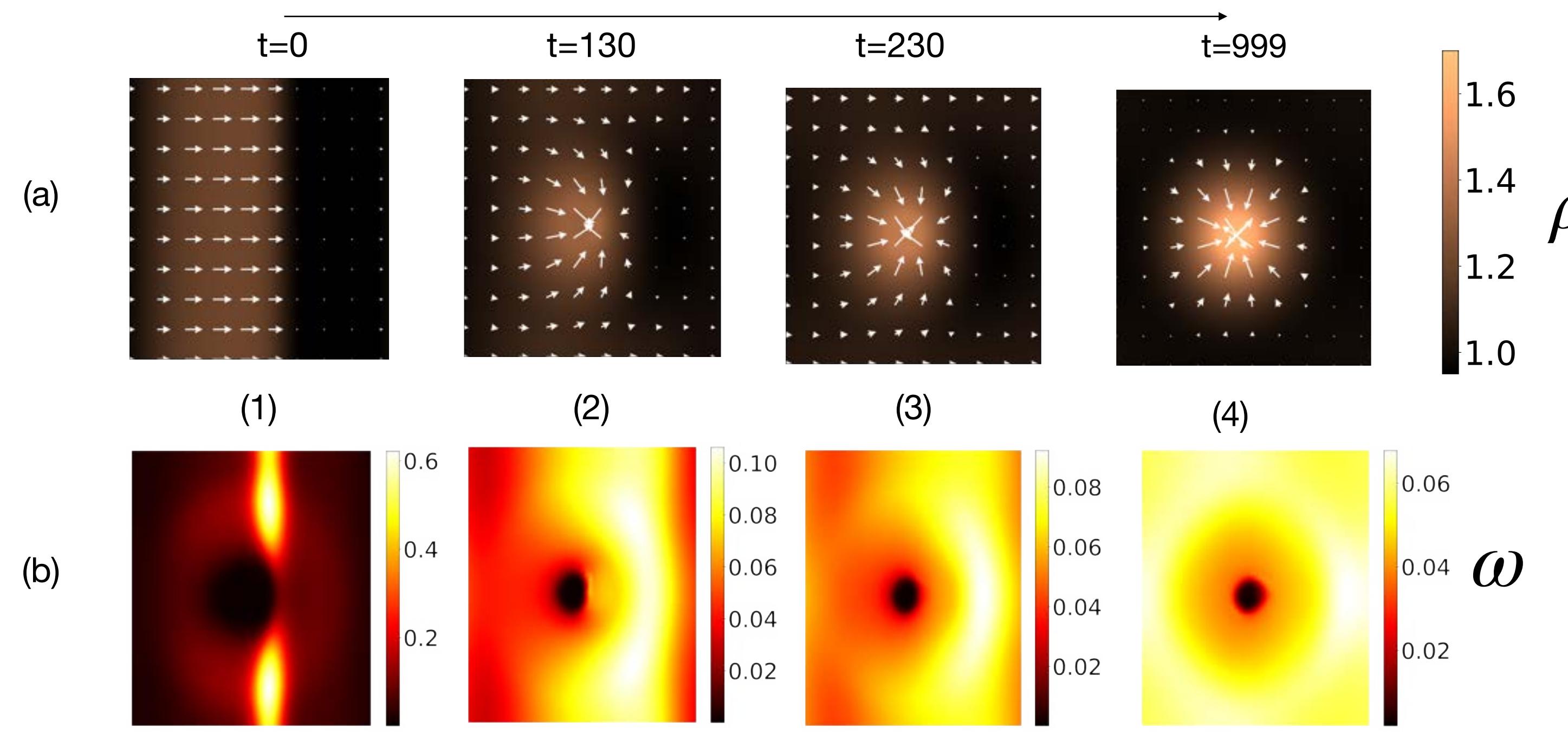
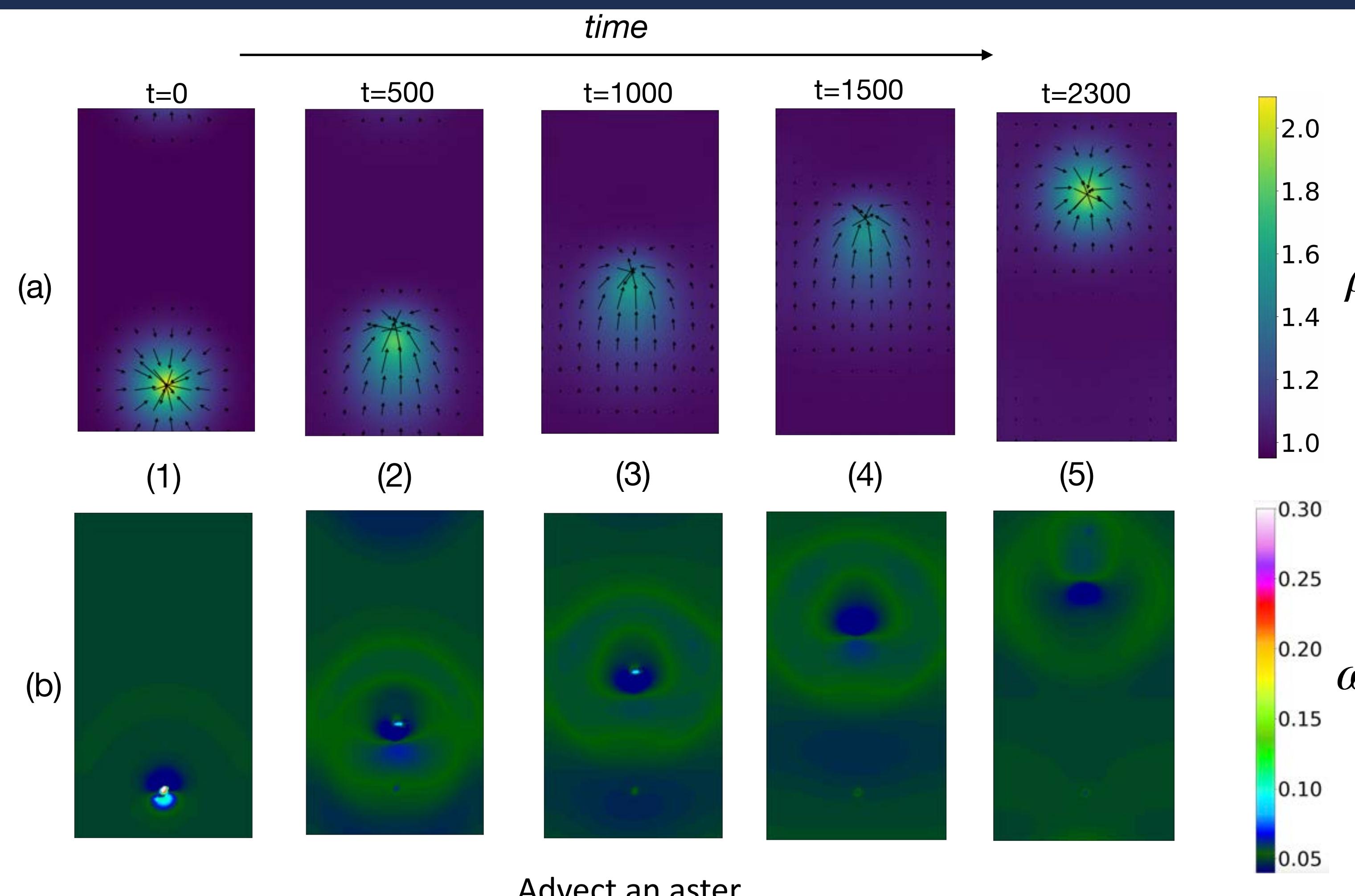
ω -activity λ -interaction



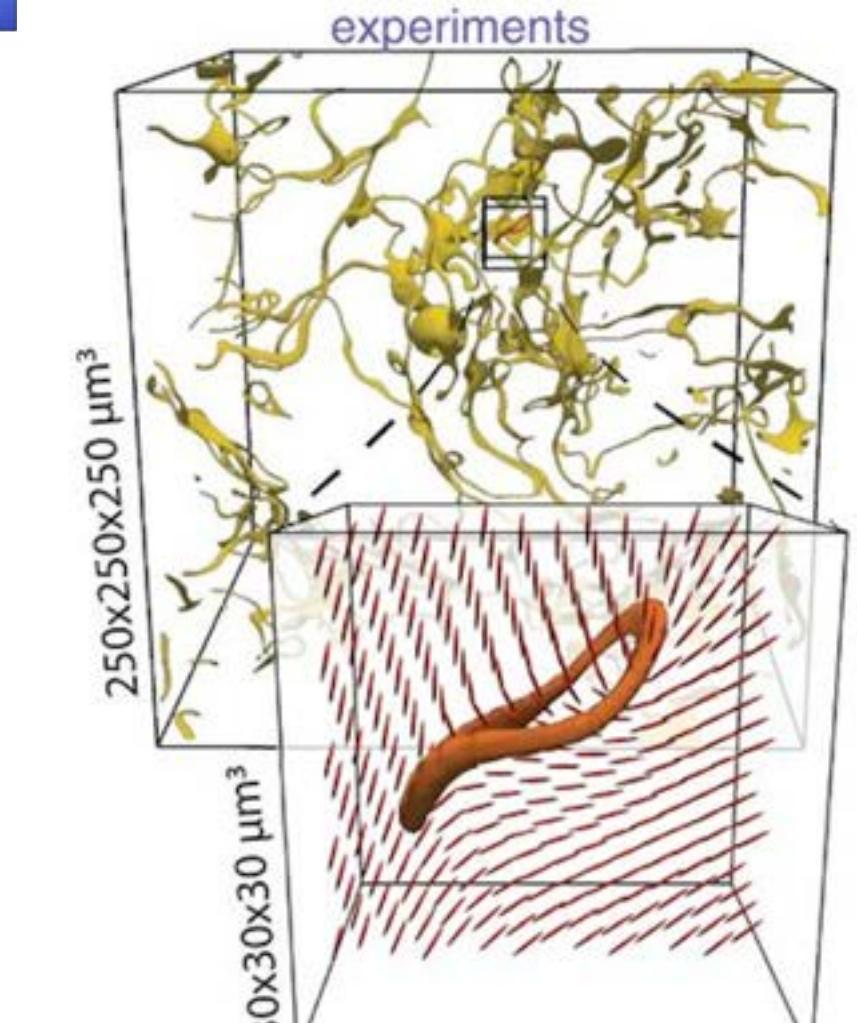
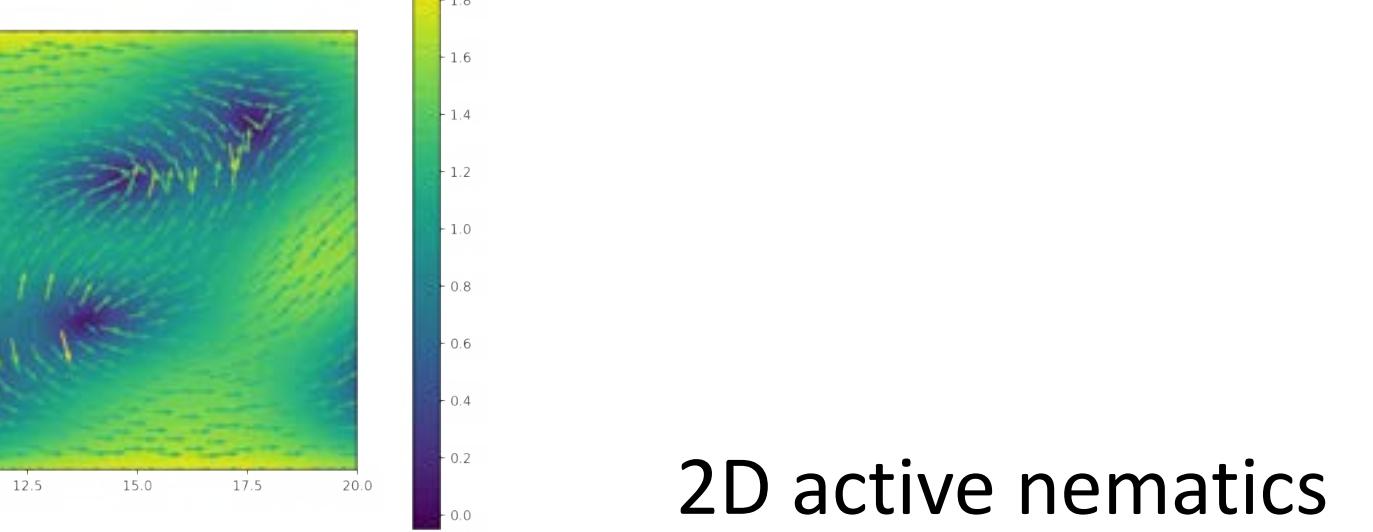
Optimal control



Results



Future Directions



References

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- A. Gopinath, M. F. Hagan, M. C. Marchetti, and A. Baskaran, Physical Review E 85, 061903 (2012).
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